# RECITAL PROCEDURES FOR SUMMER AIR CONDITIONER WITH PRE-EMPTIVE REPEAT REPAIR 

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#### Abstract

: In this paper, the author has considered a summer air conditioning system for a place in hot and dry weather. The author has computed the availability and profit function for this system. Such systems are used for hot and dry outdoor conditions like Nagpur, Delhi, Bhopal and other place. The comfort conditions required in an air-conditioned space are $24^{\circ} \mathrm{C}$ DBT (dry bulb temperature) and $60 \% \mathrm{RH}$ (relative humidity). The whole system is divided into five subsystems namely A, B, C, D and E. These subsystems are air dampers, air filter, cooling coils, adiabatic humidifier and water eliminator, respectively. All these subsystems are connected in series. The whole system reaches to failed state on failure of any of its subsystems A, C, D and E. On the other hand, the whole system works in reduced efficiency on failure of subsystems B. The whole system can also be failed due to wear-out reasons.


KEY WORDS: air filter, cooling coils, adiabatic humidifier and water eliminator

## INTRODUCTION :

In this paper, the author has considered a summer air conditioning system for a place in hot and dry weather. The author has computed the availability and profit function for this system. Such systems are used for hot and dry outdoor conditions like Nagpur, Delhi, Bhopal and other place. The comfort conditions required in an air-conditioned space are $24^{\circ} \mathrm{C}$ DBT (dry bulb temperature) and $60 \% \mathrm{RH}$ (relative humidity). The arrangement of equipments required for an ordinary system has been shown in fig-1.
The whole system is divided into five subsystems namely A, B, C, D and E. These subsystems are air dampers, air filter, cooling coils, adiabatic humidifiers and water eliminator, respectively. All these subsystems are connected in series. The whole system reaches to failed state on failure of any of its subsystems A, C, D and E. On the other hand, the whole system works in reduced efficiency on failure of subsystems B. The whole system can also be failed due to wear-out reasons. Transition-state diagram for considered system has been shown in fig-2.
Since the system under consideration is of Non-Markovian nature, the author has been used supplementary variables to convert this into Markovian. Probability considerations and limiting procedure have been used for mathematical formulations of the system. This mathematical model has been solved by using Laplace transform, to obtain probabilities of various transition states depicted in fig-2.
All failures follow exponential time distribution whereas all repairs follow general time distribution. Preemptive repeat policy has been adopted for repair purpose.
Asymptotic behavior and a particular case, when repairs follow exponential time distribution, have been computed to enhance practical utility of the system. Reliability, availability and M.T.T.F. for considered system have been obtained.
Graphical illustration followed by a numerical computation has also been appended in last to highlight important results of this paper.

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Fig-1: Summer Air conditioning system for hot and dry weather


Fig-2 : State-transition diagram

## ASSUMPTIONS:

The following assumptions have been taken care throughout:

- Initially, the whole system is operable.
- All failures follow exponential time distribution and are S-independent.
- Repairs follow general time distribution and are perfect.
- Repair facilities are always available.
- The whole system can fail either due to failure of any of its constituent subsystem or due to wear - out.
- On failure of subsystem B, the whole system works in reduced efficiency state.
- Pre-emptive repeat policy has been adopted for repair purpose.


## NOTATIONS USED:

The following notations have been used throughout in this paper:
$f_{i} \quad: \quad$ Failure rates of subsystem i.
$r_{i}(j) \Delta \quad: \quad$ First order probability that $i^{t h}$ failure can be repaired in the time interval $(j, j+\Delta)$ conditioned that it was not repaired upto time j .
$P_{0}(t) \quad: \quad \operatorname{Pr}\{$ at time t, the whole system is operable $\}$.
$P_{i}(j, t) \Delta \quad: \quad \operatorname{Pr}\left\{\right.$ at time t, system suffers with $i^{\text {th }}$ failure $\}$. Elapsed repair time lies in the interval $(j, j+\Delta)$.
$P_{W}(u, t) \Delta \quad: \quad \operatorname{Pr}\{$ at time t , system is failed due to wear-out $\}$. Elapsed repair time lies in the interval $(u, u+\Delta)$.
$P_{B i}(j, t) \Delta \quad: \quad \operatorname{Pr}\left\{\right.$ at time t , system is failed due to $i^{\text {th }}$ failure while the subsystem B has already failed $\}$. Elapsed repair time for subsystem i lies in the intervals $(j, j+\Delta)$.
$S_{i}(j)$ : $\mu_{i}(j) \exp \left\{-\int r_{i}(j) d j\right\}$,
$D_{i}(j)$
: $1-\bar{S}_{i}(j) / j, \forall i$ and j .
M.T.T.F $\quad: \quad$ Mean time to failure.

## FORMULATION OF MATHEMATICAL MODEL:

Using probability considerations and limiting procedure, we obtain the following set of difference-differential equations which is continuous in time, discrete in space and governing the behavior of considered system:

$$
\begin{align*}
{\left[\frac{d}{d t}+f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+\right.} & \left.f_{W_{1}}\right] \\
& P_{0}(t)=\int_{0}^{\infty} P_{A}(x, t) r_{A}(x) d x+\int_{0}^{\infty} P_{B}(y, t) r_{B}(y) d y \\
& +\int_{0}^{\infty} P_{C}(z, t) r_{C}(z) d z+\int_{0}^{\infty} P_{D}(m, t) r_{D}(m) d m  \tag{1}\\
& +\int_{0}^{\infty} P_{E}(n, t) r_{E}(n) d n+\int_{0}^{\infty} P_{W}(u, t) r_{W}(u) d u
\end{align*}
$$

$\left[\frac{\partial}{\partial j}+\frac{\partial}{\partial t}+r_{i}(j)\right] P_{i}(j, t)=0$
where $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}, \mathrm{E}$ and $\mathrm{j}=\mathrm{x}, \mathrm{z}, \mathrm{m}, \mathrm{n}$ respectively.
$\left[\frac{\partial}{\partial u}+\frac{\partial}{\partial t}+r_{W}(u)\right] P_{W}(u, t)=0$
$\left[\frac{\partial}{\partial y}+\frac{\partial}{\partial t}+f_{A}+f_{C}+f_{D}+f_{E}+f_{W_{2}}+r_{B}(y)\right] P_{B}(y, t)=0$
$\left[\frac{\partial}{\partial j}+\frac{\partial}{\partial t}+r_{i}(j)\right] P_{B i}(j, t)=0$
where $i=A, C, D, E$ and $j=x, z, m, n$ respectively.

## Boundary conditions are:

$P_{i}(0, t)=f_{i} P_{0}(t), \quad$ where $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
$P_{W}(0, t)=f_{W_{1}} P_{0}(t)+f_{W_{2}} P_{B}(t)$
$P_{B}(0, t)=\int_{0}^{\infty} P_{B A}(x, t) r_{A}(x) d x+\int_{0}^{\infty} P_{B C}(z, t) r_{C}(z) d z$
$+\int_{0}^{\infty} P_{B D}(m, t) r_{D}(m) d m+\int_{0}^{\infty} P_{B E}(n, t) r_{E}(n) d n+f_{B} P_{0}(t)$
$P_{B i}(0, t)=f_{i} P_{B}(t) \quad$ where $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
Initial conditions are:
$P_{0}(0)=1$, otherwise zero

## SOLUTION OF THE MODEL:

In order to solve the above set of equations to obtain different state probabilities, taking Laplace transforms of equations (1) through (9) subjected to initial conditions (10), we get:
$\left[s+f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}\right] \bar{P}_{0}(s)=1+\int_{0}^{\infty} \bar{P}_{A}(x, s) r_{A}(x) d x+\int_{0}^{\infty} \bar{P}_{B}(y, s) r_{B}(y) d y$
$+\int_{0}^{\infty} \bar{P}_{C}(z, s) r_{C}(z) d z+\int_{0}^{\infty} \bar{P}_{D}(m, s) r_{D}(m) d m \quad+\int_{0}^{\infty} \bar{P}_{E}(n, s) r_{E}(n) d n+\int_{0}^{\infty} \bar{P}_{W}(u, s) r_{W}(u) d u$
$\left[\frac{\partial}{\partial j}+s+r_{i}(j)\right] \bar{P}_{i}(j, s)=0$
where $i=A, C, D, E$ and $j=x, z, m, n$ respectively.
$\left[\frac{\partial}{\partial u}+s+r_{W}(u)\right] \bar{P}_{W}(u, s)=0$
$\left[\frac{\partial}{\partial y}+s+f_{A}+f_{C}+f_{D}+f_{E}+f_{W_{2}}+r_{B}(y)\right] \bar{P}_{B}(y, s)=0$
$\left[\frac{\partial}{\partial j}+s+r_{i}(j)\right] \bar{P}_{B i}(j, s)=0$
where $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}, \mathrm{E}$ and $\mathrm{j}=\mathrm{x}, \mathrm{z}, \mathrm{m}, \mathrm{n}$ respectively.
$\bar{P}_{i}(0, s)=f_{i} \bar{P}_{0}(s), \quad$ where $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
$\bar{P}_{W}(0, s)=f_{W_{1}} \bar{P}_{0}(s)+f_{W_{2}} \bar{P}_{B}(s)$
$\bar{P}_{B}(0, s)=f_{B} \bar{P}_{0}(s)+\int_{0}^{\infty} \bar{P}_{B A}(x, s) r_{A}(x) d x+\int_{0}^{\infty} \bar{P}_{B C}(z, s) r_{C}(z) d z$
$\bar{P}_{B i}(0, s)=f_{i} \bar{P}_{B}(s) \quad$ where $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
Now integrate equation (12) by using boundary conditions (16), we have
$\bar{P}_{i}(j, s)=f_{i} \bar{P}_{0}(s) \exp \left\{-s j-\int r_{i}(j) d j\right\}$
integrating this again w.r.t. ' j ' from 0 to $\infty$, we get
$\bar{P}_{i}(s)=f_{i} \bar{P}_{0}(s) \frac{1-\bar{S}_{i}(s)}{s}$
or, $\bar{P}_{i}(s)=f_{i} \bar{P}_{0}(s) D_{i}(s) \quad$ for $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
Similarly, equation (13) gives on integration subjected to boundary condition (17):
$\bar{P}_{W}(s)=\left[f_{W_{1}} \bar{P}_{0}(s)+f_{W_{2}} \bar{P}_{B}(s)\right] D_{W}(s)$
Integrate (15) by making use of (19), we obtain
$\bar{P}_{B i}(j, s)=f_{i} \bar{P}_{B}(s) \exp \left\{-s j-\int r_{i}(j) d j\right\}$
integrating this again w.r.t. j from 0 to $\infty$, we have
$\bar{P}_{B i}(s)=f_{i} \bar{P}_{B}(s) D_{i}(s) \quad$ for $\mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
Now simplifying (18) subjected to relevant relations, we get
$\bar{P}_{B}(0, s)=f_{B} \bar{P}_{0}(s)+f_{A} \bar{P}_{B}(s) \bar{S}_{A}(s)+f_{C} \bar{P}_{B}(s) \bar{S}_{C}(s)+f_{D} \bar{P}_{B}(s) \bar{S}_{D}(s)$
$+f_{E} \bar{P}_{B}(s) \bar{S}_{E}(s)$
Equation (14) gives on integration:
$\bar{P}_{B}(y, s)=\bar{P}_{B}(0, s) \exp \left\{-\left(s+f_{A}+f_{C}+f_{D}+f_{E}+f_{W_{2}}\right) y-\int r_{B}(y) d y\right\}$
integrating this again w.r.t. y from 0 to $\infty$, we obtain
$\bar{P}_{B}(s)=\bar{P}_{B}(0, s) D_{B}\left(s+f_{A}+f_{C}+f_{D}+f_{E}+f_{W_{2}}\right)$
or, $\bar{P}_{B}(s)=\bar{P}_{B}(0, s) D_{B}(N)$
where, $N=s+f_{A}+f_{C}+f_{D}+f_{E}+f_{W_{2}}$
using (23), it gives
$\bar{P}_{B}(s)\left[1-\left\{f_{A} \bar{S}_{A}(s)+f_{C} \bar{S}_{C}(s)+f_{D} \bar{S}_{D}(s)+f_{E} \bar{S}_{E}(s)\right\} D_{B}(N)\right]=f_{B} \bar{P}_{0}(s) D_{B}(N)$
$\therefore \bar{P}_{B}(s)=\frac{f_{B} D_{B}(N) \bar{P}_{0}(s)}{1-\left\{f_{A} \bar{S}_{A}(s)+f_{C} \bar{S}_{C}(s)+f_{D} \bar{S}_{D}(s)+f_{E} \bar{S}_{E}(s)\right\} D_{B}(N)}$
or, $\bar{P}_{B}(s)=A(s) \bar{P}_{0}(s)$
(Say)
Finally, simplifying equation (11) with the help of relevant expressions, we have
$\bar{P}_{0}(s)=\frac{1}{C(s)}$
Thus, we obtain the following L.T. of various state probabilities, depicted in fig-2, in terms of $\mathrm{C}(\mathrm{s})$ :
$\bar{P}_{0}(s)=\frac{1}{C(s)}$
$\bar{P}_{i}(s)=\frac{f_{i} D_{i}(s)}{C(s)} \quad, \quad \mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
$\bar{P}_{W}(s)=\frac{1}{C(s)}\left[f_{W_{1}}+f_{W_{2}} A(s)\right] D_{W}(s)$
$\bar{P}_{B}(s)=\frac{A(s)}{C(s)}$
$\bar{P}_{B i}(s)=\frac{f_{i} A(s) D_{i}(s)}{C(s)} \quad, \quad \mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
where, $A(s)=\frac{f_{B} D_{B}(N)}{1-\left\{f_{A} \bar{S}_{A}(s)+f_{C} \bar{S}_{C}(s)+f_{D} \bar{S}_{D}(s)+f_{E} \bar{S}_{E}(s)\right\} D_{B}(N)}$

$$
\begin{equation*}
N=s+f_{A}+f_{C}+f_{D}+f_{E}+f_{W_{2}} \tag{31}
\end{equation*}
$$

and $C(s)=s+f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}-f_{A} \bar{S}_{A}(s)-f_{C} \bar{S}_{C}(s)-f_{D} \bar{S}_{D}(s)$

$$
\begin{array}{r}
-f_{E} \bar{S}_{E}(s)-\left[f_{W_{1}}+f_{W_{2}} A(s)\right] \bar{S}_{W}(s) \\
-\left[f_{B}+\left\{f_{A} \bar{S}_{A}(s)+f_{C} \bar{S}_{C}(s)+f_{D} \bar{S}_{D}(s)+f_{E} \bar{S}_{E}(s)\right\} A(s)\right] \bar{S}_{B}(N) \tag{32}
\end{array}
$$

## VERIFICATION:

It is interesting to note here that
sum of equations (25) through (29) $=\frac{1}{s}$

## STEADY-STATE BEHAVIOUR OF THE SYSTEM:

Using final value theorem in L.T., viz, $\lim _{t \rightarrow \infty} P(t)=\lim _{s \rightarrow 0} s \bar{P}(s)=P($ say $)$, provided the limit on LHS exists, in equations (25) through (29), we obtain the following steady-state behavior of the considered system:
$P_{0}=\frac{1}{C^{\prime}(0)}$
$P_{i}=\frac{f_{i} M_{i}}{C^{\prime}(0)} \quad, \quad \mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
$P_{W}=\frac{1}{C^{\prime}(0)}\left[f_{W_{1}}+f_{W_{2}} A(0)\right] M_{W}$
$P_{B}=\frac{A(0)}{C^{\prime}(0)}$
$P_{B i}=\frac{f_{i} A(0) M_{i}}{C^{\prime}(0)}, \quad \mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
where, $C^{\prime}(0)=\left[\frac{d}{d s} C(s)\right]_{s=0}$
$M_{i}=-\bar{S}_{i}^{\prime}(0)=$ mean time to repair $i^{\text {th }}$ failure.
and $A(0)=\frac{f_{B} D_{B}(N-s)}{1-\left(f_{A}+f_{C}+f_{D}+f_{E}\right) D_{B}(N-s)}$

## PARTICULAR CASE:

When repairs follow exponential time distribution
In this case, setting $\bar{S}_{i}(j)=\frac{r_{i}}{j+r_{i}}, \forall i$ and $j$ in equations (25) through (29) we obtain the following L.T. of various states probabilities of fig-2:
$\bar{P}_{0}(s)=\frac{1}{E(s)}$
$\bar{P}_{i}(s)=\frac{f_{i}}{E(s)\left(s+r_{i}\right)} \quad, \quad \mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
$\bar{P}_{W}(s)=\frac{1}{E(s)}\left[f_{W_{1}}+f_{W_{2}} Q(s)\right] \frac{1}{s+r_{W}}$
$\bar{P}_{B}(s)=\frac{Q(s)}{E(s)}$
$\bar{P}_{B i}(s)=\frac{f_{i} Q(s)}{E(s)\left(s+r_{i}\right)} \quad, \quad \mathrm{i}=\mathrm{A}, \mathrm{C}, \mathrm{D}$ and E
where, $Q(s)=\frac{f_{B}\left[1-\bar{S}_{B}(N)\right]}{N-\left(\frac{f_{A} r_{A}}{s+r_{A}}+\frac{f_{C} r_{C}}{s+r_{C}}+\frac{f_{D} r_{D}}{s+r_{D}}+\frac{f_{E} r_{E}}{s+r_{E}}\right)\left[1-\bar{S}_{B}(N)\right]}$
and $E(s)=s+f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}-\frac{f_{A} r_{A}}{s+r_{A}}-\frac{f_{C} r_{C}}{s+r_{C}}-\frac{f_{D} r_{D}}{s+r_{D}}-\frac{f_{E} r_{E}}{s+r_{E}}$

$$
\begin{align*}
& -\left[f_{W_{1}}+f_{W_{2}} Q(s)\right] \frac{r_{W}}{s+r_{W}} \\
- & {\left[f_{B}+\left\{\frac{f_{A} r_{A}}{s+r_{A}}+\frac{f_{C} r_{C}}{s+r_{C}}+\frac{f_{D} r_{D}}{s+r_{D}}+\frac{f_{E} r_{E}}{s+r_{E}}\right\} Q(s)\right] \frac{r_{B}}{N+r_{B}} }
\end{align*}
$$

N has been mentioned earlier in equation (31).
RELIABILITY AND M.T.T.F. OF THE SYSTEM:
We have from equation (25)
$\bar{R}(s)=\frac{1}{s+f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}}$
Taking inverse L.T., we get
$R(t)=\exp \left\{-\left(f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}\right) t\right\}$
Also, M.T.T.F. $=\int_{0}^{\infty} R(t) d t$

$$
\begin{equation*}
=\frac{1}{f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}} \tag{47}
\end{equation*}
$$

## AVAILABILITY OF THE SYSTEM:

From equations (25) and (28), we obtain

$$
\bar{P}_{u p}(s)=\frac{1}{s+f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}}\left[1+\frac{f_{B}}{s+f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{2}}}\right]
$$

Taking inverse L.T., we get

$$
\begin{gather*}
P_{u p}(t)=\left(1+\frac{f_{B}}{f_{W_{2}}-f_{B}-f_{W_{1}}}\right) \exp \left\{-\left(f_{A}+f_{B}+f_{C}+f_{D}+f_{E}+f_{W_{1}}\right) t\right\} \\
-\frac{f_{B}}{f_{W_{2}}-f_{B}-f_{W_{1}}} \exp \left\{-\left(f_{A}+f_{C}+f_{D}+f_{E}+f_{W_{2}}\right) t\right\} \tag{48}
\end{gather*}
$$

Again, $P_{\text {down }}(t)=1-P_{u p}(t)$
NUMERICAL COMPUTATON:
For a numerical computation, let us consider the following values:
$f_{A}=0.001, f_{B}=0.002, f_{C}=0.06, f_{D}=0.04, f_{E}=0.008, f_{W_{1}}=0.003, f_{W_{2}}=0.009$ and $t=0,1,2,--$.

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Using these values in equations (46), (47) and (48) we obtain the table-1, 2 and 3 , respectively. The corresponding graphs have been shown in fig-2, 3 and 4 respectively.

Table-1

| $\mathbf{t}$ | $\mathbf{R}(\mathbf{t})$ |
| :--- | :--- |
| 0 | 1 |
| 1 | 0.892258 |
| 2 | 0.796124 |
| 3 | 0.710348 |
| 4 | 0.633814 |
| 5 | 0.565525 |
| 6 | 0.504595 |
| 7 | 0.450229 |
| 8 | 0.40172 |
| 9 | 0.358438 |
| 10 | 0.319819 |



Fig-3

Table-2

| $\mathbf{t}$ | $\mathbf{P}_{\text {up }}(\mathbf{t})$ |
| :--- | :--- |
| 0 | 1 |
| 1 | 0.894039 |
| 2 | 0.799296 |
| 3 | 0.714585 |
| 4 | 0.638844 |
| 5 | 0.571125 |
| 6 | 0.510578 |
| 7 | 0.456444 |
| 8 | 0.408046 |
| 9 | 0.364775 |
| 10 | 0.326089 |

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Fig-4

Table-3

| $\mathbf{f}_{\boldsymbol{B}}$ | M.T.T.F $\boldsymbol{\theta}$ |
| :--- | :--- |
| 0 | 8.928571 |
| 0.001 | 8.849558 |
| 0.002 | 8.77193 |
| 0.003 | 8.695652 |
| 0.004 | 8.62069 |
| 0.005 | 8.547009 |
| 0.006 | 8.474576 |
| 0.007 | 8.403361 |
| 0.008 | 8.333333 |
| 0.009 | 8.264463 |
| 0.01 | 8.196721 |



Fig-5

## RESULTS AND DISCUSSION:

Table-1 gives the values of reliability of considered system for various values of time $t$. Its graph has been shown in fig-3. Analysis of table-1 and fig-3 reveal that the reliability of considered system decreases approximately in constant manner and there are no sudden jumps in the values of reliability.
Table-2 gives the values of availability of considered system for different values of time $t$. Its graph has been shown in fig-4. Critical examination of table-2 and fig-4 yield that value of availability decreases rapidly in the beginning but thereafter it decreases constantly.
Table-3 gives the values of M.T.T.F. of considered system for different values of failure rate of subsystem B. Its graph has been shown in fig-2. Analysis of table-3 and fig-5 yield that value of M.T.T.F. decreases catastrophically.

## REFERENCES:

1. Chung, W. K.: "A k-out -of n: G Redundant System with the Presence of Chance with Multiple Critical Errors", Microelectronic Reliab. , Vol. 33, pp 334-338, 2012.
2. Chung, W. K.: " Reliability Analysis of a k-out -of n: G Redundant System in the Presence of Chance with Multiple Critical Errors", Microelectronic Reliab. , Vol. 32, pp 331-334, 2010.
3. Dhillon, B. S. and Yang N. J.: "Stochastic Analysis of Standby System with Common Cause Failure and Human Error", Microelectronic Reliab. , Vol. 32, pp 1699-1712, 2012.
4. Gupta, P.P.; Sharma, R.K.: "Cost Analysis of Three-state Standby Redundant Electronic Equipment", Microelectronic Reliab. , Vol. 25, pp 1029-1033, 2005.
5. Gupta, P.P.; Kumar, A.; Mittal, S.K.: "Stochastic Behaviour of Three-State Complex Repairable System with Three Types of Failures", Microelectronic Reliab., Vol. 25, pp 853-858, 2004.
6. Hyderi, P. D.; Joorel , J. P. S. : "Stochastic Behaviour of a Two Unit Cold Standby Redundant System Subject to Random Failure", Microelectronic Reliab., Vol. 36(2), pp 243 - 246, 2007.
7. Jen - Shyan, W.; Rong - Jaye, C.: 'Efficient Algorithm for Reliability of a Circular Consecutive k-out-of-n: F System", IEEE TR on Reliability, Vol. 55, issue - 1, pp 163-164, 2014.
8. Mittal, S. K.; Gupta, P.P.: "Complex System with Delayed Repair", IEEE Trans. On Reliability, Vol. R - 31, No. 3, 2004.
9. Mittal, S. K.; Gupta, P.P.: "Operational Availability of a Complex Redundant System with Waiting and Environmental Effects", Quality and Reliability Journal, Vol. 9, No. 1, pp 13 - 16, 2001.
10. Parashar, B.; Taneja, G.: "Reliability and Profit Evaluation of a PLC Hot Standby System Based on a Master-Slave Concept and Two Types of Repair Facilities", IEEE TR. on Reliability, Vol. 56 (3), pp 534-539, 2013.
11. Tang, Y.H.: "Some New Reliability Problems and Results for One Unit Repairable System", Microelectronic Reliab. , Vol. 36 (4), pp 465-468, 2004.
12. Wang, K.H.; Hsu, L. Y.: "Cost Analysis of the Machine Repair Problem with Reliability Non-Reliable Service Stations", Microelectronic Reliab., Vol. 35 (6), pp 923-934, 2013.
13. Zhang, Y.L.; Wang, T. P.: "Reliability Consecutive 2 -out of $\mathrm{N}: F \mathrm{~F}$ System", Microelectronic Reliab. , Vol. 36 (5), pp 605608, 2001.
